



## **Estimation of luminous efficacy of daylight and illuminance for composite climate**

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### **Abstract**

This Daylighting is one of the basic components of passive solar building design and its estimation is essential. In India there are a few available data of measured illuminance as in many regions of the world. The Indian climate is generally clear with overcast conditions prevailing through the months of July to September, which provides good potential to daylighting in buildings. Therefore, an analytical model that would encompass the weather conditions of New Delhi was selected. Hourly exterior horizontal and slope daylight availability has been estimated for New Delhi using daylight modeling techniques based on solar radiation data. A model to estimate interior illuminance was investigated and validated using experimental hourly inside illuminance data of an existing skylight integrated vault roof mud house in composite climate of New Delhi. The interior illuminance model was found in good agreement with experimental value of interior illuminance.

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**Keywords:** Global, Diffuse, Efficacy, Irradiance, Illuminance.

### **1. Introduction**

Optimal utilization of daylight can attribute to significant amount of energy savings. Studies do reveal that if daylighting were used for illumination purposes adequately it would reduce the energy consumption in our households. As buildings are architectural elements that are exposed to the sun, prediction of daylight availability in them is required. The availability of daylight for exterior illuminance is a field of study considerably different from the measurement and simulation of solar radiation [1]. Solar radiation is the total incident energy visible and invisible from the sun and daylight is the visible portion of this electromagnetic radiation as perceived by the eye. The task is to isolate this portion from the total energy. Using established models it is possible to predict the Luminous Efficacy and then estimate the monthly mean of hourly exterior illuminance (diffuse, direct and global) on horizontal and for all the four walls (N-S-E-W) of any building in the region.

This paper investigates experimentally the skylight rooms to validate the proposed interior illuminance model which is based on conservation of illuminance. The vertical height considered for the study is 75 cm above floor level which corresponds to working on table by sitting on chair.

The hourly experimental data of illuminance level inside were measured on typical days in each month of the year for small and big dome rooms of the existing skylight building located in New Delhi composite climate. The importance of skylight was presented in this paper by evaluating the artificial lighting energy saving potential and corresponding CO<sub>2</sub> mitigation potential to elaborate the effect of daylighting in climate change mitigation. The carbon credit earning potential of skylight integrated dome shaped roof

room was also evaluated. The objective of paper is to introduce the importance of daylighting in building using actual measured data in India especially in New Delhi city and validation of interior illuminance model.

## 2. Location and climatic conditions

New Delhi is located in Northern part of India, a latitude  $28.58^{\circ}$  N and a longitude of  $77.02^{\circ}$  E and at an altitude of 216m above M.S.L. The climate of Delhi is a monsoon-influenced humid subtropical climate (Koppen climate classification Cwa) with high variation between summer and winter temperatures and precipitation. Summers start in early April and peak in May, with average temperatures near  $32^{\circ}\text{C}$  ( $90^{\circ}\text{F}$ ), although occasional heat waves can result in highs close to  $45^{\circ}\text{C}$  ( $114^{\circ}\text{F}$ ) on some days. The monsoon starts in late June and lasts until mid-September, with about 714 mm (28.1 inches) of rain. The average temperatures are around  $29^{\circ}\text{C}$  ( $85^{\circ}\text{F}$ ), although they can vary from around  $25^{\circ}\text{C}$  ( $78^{\circ}\text{F}$ ) on rainy days to  $32^{\circ}\text{C}$  ( $90^{\circ}\text{F}$ ) during dry spells. The monsoons recede in late September, and the post-monsoon season continues till late October, with average temperatures sliding from  $29^{\circ}\text{C}$  ( $85^{\circ}\text{F}$ ) to  $21^{\circ}\text{C}$  ( $71^{\circ}\text{C}$ ).

Winter starts in November and peaks in January, with average temperatures around  $12\text{--}13^{\circ}\text{C}$  ( $54\text{--}55^{\circ}\text{F}$ ). Although winters are generally mild, Delhi's proximity to the Himalayas results in cold waves that regularly dip temperatures below freezing. Delhi is notorious for its heavy fog during the winter season. In December, reduced visibility leads to disruption of road, air and rail traffic. They end in early February, and are followed by a short spring till the onset of the summer. Extreme temperatures have ranged from  $-0.6^{\circ}\text{C}$  ( $30.9^{\circ}\text{F}$ ) to  $47^{\circ}\text{C}$  ( $116.6^{\circ}\text{F}$ ).

## 3. Estimation of luminous efficacy and horizontal exterior illuminance

Researchers have investigated the relation between solar radiation and daylight and proposed various mathematical models relating the two [2–7]. The model proposed by Perez and others [4] is usually considered to be most accurate and was selected to predict hourly Luminous Efficacy, horizontal and slope illuminance values for the 12 months of a year. The model has been validated by data from different location with a very good agreement [8,9].

According to this model, the global ( $K_g$ ) and diffuse ( $K_d$ ) efficacies can be found by the following equation [4]:

$$K_g \text{ or } K_d = a_i + b_i W + c_i \cos(z) + d_i \ln(\Delta) \quad (1)$$

where  $a_i$ ,  $b_i$ ,  $c_i$  and  $d_i$  are given coefficients (for diffuse or global efficacies), Table 1, corresponding to the sky's clearness ( $\varepsilon$ ),  $W$  is the atmospheric precipitable water content; ( $\Delta$ ) is the sky brightness.

The sky clearness ( $\varepsilon$ ) for irradiance is given by

$$\varepsilon = [(I_d + I_n) / I_d + 1.041z^3] / [1 + 1.041z^3] \quad (2)$$

where  $I_d$  is the horizontal diffuse irradiance,  $I_n$  is the normal incidence direct irradiance;  $z$  is the solar zenith angle in radians.

The zenith angle is calculated through

$$\cos z = \cos \phi \cos \delta \cos \omega + \sin \phi \sin \delta \quad (3)$$

where  $\phi$  is the latitude, and  $\delta$  is the solar declination, which can be expressed as

$$\delta = 23.45 \sin \left[ \frac{360}{365} (284 + n) \right] \quad (4)$$

where  $n$  is the day of the year given for each month in Table 2 [10],  $\omega$  is the hour angle:

$$\omega = (ST - 12)15^{\circ} \quad (5)$$

where  $ST$  is the solar time for our calculations.

$$I_n = I_b / \cos z \quad (6)$$

where  $I_b$  is the horizontal beam irradiance.

The sky brightness ( $\Delta$ ) is given by

$$\Delta = I_d m / I_{on} \quad (7)$$

where  $m$  is the optical air mass;  $I_{on}$  is the extraterrestrial normal incidence irradiance.  $m$  was obtained from Kasten's [11] formula, which provides an accuracy of 99.6% for zenith angles up to  $89^\circ$ .

$$m = [\cos z + 0.15 \times (93.885 - z)^{-1.253}]^{-1} \quad (8)$$

Eq. (8) is applicable to a standard pressure  $p_0$  of 1013.25 mbar at sea level. For other pressures the air mass is corrected by;

$$m' = m(p / 1013.25) \quad (9)$$

where  $p$  is the atmospheric pressure in mbar at height  $h$  meters above sea level,  $p$  was estimated by formula given by Lunde [12],

$$p / p_0 = \exp(-0.0001184h) \quad (10)$$

The atmospheric perceptible water content (cm), is given by Wright et al. [13]:

$$W = \exp(0.07T_d - 0.075) \quad (11)$$

where  $T_d$  is the hourly surface dew-point temperature ( $^\circ\text{C}$ ).  $T_d$  can be expressed by Magnus-Tetens formulation [14].

For  $0^\circ\text{C} < T < 60^\circ\text{C}$ ,  $0.01 < RH < 1.00$ ,  $0^\circ\text{C} < T_d < 50^\circ\text{C}$ ,

$$T_d = b\alpha / a - \alpha, \quad (12)$$

$$\alpha = aT / b + T + \ln(RH) \quad (13)$$

where  $a=17.27$  and  $b=237.7^\circ\text{C}$ ,  $T$  in  $^\circ\text{C}$  is the measured temperature and  $RH$  is the measured relative humidity.

The extraterrestrial normal incidence irradiance  $I_{on}$  can be calculated by

$$I_{on} = 1367[1.0 + 0.033 \cos(360n / 365)] \quad (14)$$

The horizontal diffuse illuminance ( $E_d$ ) and the horizontal global illuminance ( $E_g$ ) can be estimated by the following:

$$E_d = I_d K_d \quad (15)$$

$$E_g = I_g K_g \quad (16)$$

Thus based on the Eqs. (1)-(16), the luminous efficacy and horizontal diffuse and global illuminance is estimated for New Delhi from the available irradiance data.

#### 4. Estimation of slope exterior illuminance

Direct illuminance on horizontal surface can be calculated from the difference between estimated values of global and diffuse illuminance on a horizontal surface.

The hourly diffuse illuminance,  $E_{\beta,d}$  on an inclined surface with a slope  $\beta$  is obtained in the simplified Perez model [4] from the following equation:

$$E_{\beta,d} = E_d[(1-F_1)(1+\cos\beta)/2 + (a_0/a_1)F_1 + F_2 \sin\beta] \quad (17)$$

where  $a_0$ ,  $a_1$  and  $\beta$  are given as;

$$a_0 = \max(0, \cos\theta), \quad a_1 = \max(0.087, \cos z), \quad \beta = 90^\circ \quad (18)$$

where  $\theta$  is the incidence angle of the sun on the surface and  $z$  the zenith angle.  $\theta$  can be calculated from the relation:

$$\begin{aligned} \cos\theta = & \sin\phi \sin\delta \cos\beta - \sin\delta \cos\phi \sin\beta \cos\gamma + \cos\phi \cos\delta \cos\omega \cos\beta \\ & + \cos\delta \sin\phi \sin\beta \cos\gamma \cos\omega + \cos\delta \sin\beta \sin\gamma \sin\omega \end{aligned} \quad (19)$$

where  $\gamma$  is the surface azimuth angle,  $E_d$  is the horizontal diffuse illuminance and  $F_1$  and  $F_2$  are coefficients, which respectively express the degree of anisotropy of the circumsolar and the horizon regions. These coefficients show a dependence on the parameters that define the sky conditions:

(a) The zenith angle,  $z$ .

(b) The clearness index  $\varepsilon'$  for illuminance is defined through:

$$\varepsilon' = [(E_d + E_n) / E_d + kz^3] / [1 + kz^3] \quad (20)$$

where  $E_n$  is the direct normal illuminance:

$$E_n = E_b / \cos z \quad (21)$$

where  $E_b$  is the horizontal beam illuminance.

(c) The sky's brightness  $\Delta'$  is defined by

$$\Delta' = E_d m / E_o \quad (22)$$

where  $E_o = 133.8$  klx is the mean extraterrestrial normal illuminance and  $m$  is the optical air mass. The model considers a set of categories for  $\varepsilon'$  and for each of them  $F_1$  and  $F_2$  are given as;

$$F_1 = F_{11} + F_{12}\Delta + F_{13}z \quad (23)$$

$$F_2 = F_{21} + F_{22}\Delta + F_{23}z \quad (24)$$

In Table 3 coefficients of Perez et al. slope illuminance model are shown. Based on Eqs. (18)–(24) hourly slope diffuse illuminance was estimated. The approach to calculate the global illuminance on a sloping surface is to first estimate the irradiance on a sloping surface and then multiply it by the global luminous efficacy. The hourly global irradiance on an inclined surface  $I_\beta$  with a slope  $\beta$  can be obtained by the following expression given by Liu and Jordan [15]

$$I_\beta = I_b R_b + I_d(1 + \cos\beta) / 2 + \rho(I_b + I_d)(1 - \cos\beta) / 2 \quad (25)$$

where  $R_b = \cos\theta / \cos z$  and  $\rho$  is the reflectivity of the ground taken as 0.2.

The global illuminance on a tilted surface  $E_{\beta,g}$  would now be;

$$E_{\beta,g} = I_\beta K_g \quad (26)$$

Table 1. Luminous efficacy coefficients of Perez et al (1990)

| S.<br>No. | $\epsilon$  |             | Global efficacy coefficients |       |       |        | Diffuse efficacy coefficients |       |        |        |
|-----------|-------------|-------------|------------------------------|-------|-------|--------|-------------------------------|-------|--------|--------|
|           | Lower bound | Upper bound | $a_i$                        | $b_i$ | $c_i$ | $d_i$  | $a_i$                         | $b_i$ | $c_i$  | $d_i$  |
| 1         | 1           | 1.065       | 96.63                        | -0.47 | 11.50 | -9.16  | 97.24                         | -0.46 | 12.00  | -8.91  |
| 2         | 1.065       | 1.230       | 107.54                       | 0.79  | 1.79  | -1.19  | 107.22                        | 1.15  | 0.59   | -3.95  |
| 3         | 1.230       | 1.500       | 98.73                        | 0.70  | 4.40  | -6.95  | 104.97                        | 2.96  | -5.53  | -8.77  |
| 4         | 1.500       | 1.950       | 92.72                        | 0.56  | 8.36  | -8.31  | 102.39                        | 5.59  | -13.95 | -13.90 |
| 5         | 1.950       | 2.800       | 86.73                        | 0.98  | 7.10  | -10.94 | 100.71                        | 5.94  | -22.75 | -23.74 |
| 6         | 2.800       | 4.500       | 88.34                        | 1.39  | 6.06  | -7.60  | 106.42                        | 3.83  | -36.15 | -28.83 |
| 7         | 4.500       | 6.200       | 78.63                        | 1.47  | 4.93  | -11.37 | 141.88                        | 1.90  | -53.24 | -14.03 |
| 8         | 6.200       | -           | 99.65                        | 1.86  | -4.46 | -3.15  | 152.23                        | 0.35  | -45.27 | -7.98  |

Table 2. Average day of each month

| Month | Date | Day of the Year |
|-------|------|-----------------|
| Jan   | 17   | 17              |
| Feb   | 16   | 47              |
| Mar   | 16   | 75              |
| Apr   | 15   | 105             |
| May   | 15   | 135             |
| Jun   | 11   | 162             |
| Jul   | 17   | 198             |
| Aug   | 16   | 228             |
| Sep   | 15   | 258             |
| Oct   | 15   | 288             |
| Nov   | 14   | 318             |
| Dec   | 10   | 344             |

Table 3. Coefficients of Perez et al. (1990) slope illuminance model

| $\epsilon'$ | 1-1.065 | 1.065-<br>1.230 | 1.230-<br>1.500 | 1.500-<br>1.950 | 1.950-<br>2.800 | 2.800-<br>4.500 | 4.500-<br>6.200 | 6.200  |
|-------------|---------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|--------|
| $F_{11}$    | 0.011   | 0.429           | 0.809           | 1.014           | 1.282           | 1.426           | 1.485           | 1.170  |
| $F_{12}$    | 0.570   | 0.363           | -0.054          | -0.252          | -0.420          | -0.653          | -1.214          | -0.300 |
| $F_{13}$    | -0.081  | -0.307          | -0.442          | -0.531          | -0.689          | -0.779          | -0.784          | -0.615 |
| $F_{21}$    | -0.095  | 0.050           | 0.181           | 0.275           | 0.380           | 0.425           | 0.411           | 0.518  |
| $F_{22}$    | 0.158   | 0.008           | -0.169          | -0.350          | -0.559          | -0.785          | -0.629          | -1.892 |
| $F_{23}$    | -0.018  | -0.065          | -0.092          | -0.096          | -0.114          | -0.097          | -0.082          | -0.055 |

## 5. Results and discussion

Tables 4 and 5 show for New Delhi the calculated monthly average of the hourly values of global and diffuse efficacies on a horizontal plane, respectively. Global luminous efficacies in July and August are found to be higher than those of the same hour in other months mainly due to high solar altitude while diffuse luminous efficacy of December month was found to be highest. The annual average efficacy under the sky conditions of the area will be useful for the architects and designers. By knowing the average radiation data, the corresponding average illumination level can be determined using these luminous efficacies.

The estimated yearly average global luminous efficacy is 108.0 lm/W and the yearly average diffuse luminous efficacy is 136.5 lm/W. Diffuse luminous efficacy is higher than the global efficacy in the sky type of the area indicating that diffuse component in daylighting design is more energy efficient.

Table 4. Average global luminous efficacy (lm/W)

| Hour | Jan | Feb | Mar | Apr | May | Jun | Jul | Aug | Sep | Oct | Nov | Dec |
|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 8    | 108 | 107 | 108 | 107 | 108 | 110 | 113 | 114 | 112 | 112 | 110 | 109 |
| 9    | 107 | 107 | 107 | 107 | 108 | 110 | 112 | 113 | 111 | 111 | 109 | 109 |
| 10   | 107 | 106 | 107 | 107 | 108 | 110 | 110 | 112 | 111 | 109 | 109 | 109 |
| 11   | 106 | 106 | 106 | 106 | 107 | 109 | 110 | 111 | 110 | 108 | 107 | 108 |
| 12   | 106 | 106 | 106 | 106 | 106 | 109 | 110 | 111 | 110 | 108 | 107 | 106 |
| 13   | 106 | 105 | 106 | 105 | 106 | 108 | 110 | 109 | 110 | 107 | 106 | 106 |
| 14   | 106 | 105 | 106 | 105 | 106 | 108 | 110 | 109 | 110 | 108 | 106 | 106 |
| 15   | 106 | 106 | 106 | 105 | 106 | 108 | 111 | 110 | 110 | 108 | 106 | 106 |
| 16   | 105 | 105 | 106 | 105 | 106 | 108 | 111 | 111 | 110 | 108 | 106 | 106 |
| 17   | 104 | 105 | 106 | 105 | 106 | 109 | 112 | 111 | 110 | 108 | 106 | 104 |

Table 5. Average diffuse luminous efficacy (lm/W)

| Hour | Jan | Feb | Mar | Apr | May | Jun | Jul | Aug | Sep | Oct | Nov | Dec |
|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 8    | 157 | 153 | 149 | 144 | 142 | 142 | 143 | 147 | 148 | 157 | 158 | 160 |
| 9    | 150 | 145 | 141 | 137 | 135 | 135 | 136 | 140 | 140 | 148 | 152 | 154 |
| 10   | 144 | 140 | 135 | 131 | 130 | 130 | 129 | 131 | 135 | 139 | 146 | 150 |
| 11   | 140 | 136 | 131 | 127 | 126 | 126 | 125 | 127 | 131 | 135 | 141 | 145 |
| 12   | 139 | 135 | 130 | 126 | 125 | 125 | 123 | 126 | 130 | 134 | 138 | 139 |
| 13   | 139 | 136 | 131 | 127 | 126 | 125 | 124 | 126 | 130 | 134 | 139 | 140 |
| 14   | 143 | 139 | 135 | 130 | 129 | 128 | 128 | 129 | 133 | 138 | 142 | 144 |
| 15   | 147 | 144 | 140 | 136 | 134 | 133 | 134 | 135 | 139 | 143 | 147 | 149 |
| 16   | 153 | 150 | 147 | 142 | 140 | 140 | 141 | 143 | 146 | 150 | 153 | 154 |
| 17   | 156 | 155 | 153 | 149 | 147 | 148 | 149 | 151 | 153 | 157 | 157 | 155 |

Figures 1 and 2 show the cumulative frequency distribution of the estimated global luminous efficacy and diffuse luminous efficacy, respectively for typical office hours from 8 am to 5 pm. The global cumulative frequency and the diffuse cumulative frequency drop rapidly from 106 to 114 lm/W and 130 to 160 lm/W respectively indicating that for most of the times of the year the luminous efficacies lie between these two values. From the energy efficiency point of view this is much better than the 16–40 lm/W for incandescent lamps and 50–80 lm/W for fluorescent lamps because there will be less heat penetration to achieve the same lighting levels as compared to electric lighting in buildings. This would also result in less cooling loads and savings in air-conditioning electric consumption.

To estimate the efficacies and illuminances, data of the hourly global and diffuse solar radiation ( $\text{W}/\text{m}^2$ ) on a horizontal surface for a period of 11 years (1991–2001) have been used. The data have been obtained from the India Meteorological Department, Pune, India. The data of hourly relative humidity was taken from Mani and Rangrajan [16].

The estimated global and diffuse horizontal illuminance data is shown in Tables 6 and 7. The maximum horizontal global illuminance is found in June month because of the higher values of solar radiation and luminous efficacy. The maximum horizontal diffuse illuminance is found in July months because of overcast conditions due to monsoons.

Graphs of illuminance against irradiance were plotted for both global and diffuse components for the location. The graphs Figures 3 and 4 confirm the linear relationship between the irradiance and illuminance.

For daylighting design considerations cumulative frequency distribution curves of illuminance outdoors was plotted to indicate the percentage of working hours in which a given illuminance is exceeded. Figures 5 and 6 show the frequency distribution for estimated outdoor global and diffuse illuminance based on office hours from 08:00 to 18:00 h. Assuming a daylight factor of 3% and the indoor design illuminance of 500 lx, the required outdoor illuminance should be 15,000 lx. From Figure 5 it can be seen that 90% of the time in a year the outdoor illuminance would be above 15,000 lx.

Table 6. Average global horizontal illuminance (lx)

| Hour | Jan   | Feb   | Mar   | Apr   | May    | Jun    | Jul   | Aug   | Sep   | Oct   | Nov   | Dec   |
|------|-------|-------|-------|-------|--------|--------|-------|-------|-------|-------|-------|-------|
| 8    | 14311 | 19339 | 28743 | 39529 | 44012  | 48183  | 41512 | 38046 | 31200 | 18889 | 13305 | 10128 |
| 9    | 38084 | 43094 | 52393 | 63018 | 65656  | 69970  | 65812 | 59832 | 55880 | 40440 | 34479 | 29918 |
| 10   | 59210 | 63219 | 71602 | 81856 | 83551  | 87864  | 81116 | 75384 | 75633 | 61604 | 52700 | 48160 |
| 11   | 72433 | 77134 | 85344 | 94256 | 96151  | 99914  | 91748 | 91207 | 89387 | 75238 | 65455 | 60991 |
| 12   | 77002 | 83082 | 91882 | 99439 | 101900 | 103353 | 96994 | 96242 | 95709 | 82096 | 70739 | 65879 |
| 13   | 77441 | 83544 | 91919 | 99483 | 101043 | 102255 | 98620 | 88369 | 94022 | 81147 | 69972 | 65389 |
| 14   | 69384 | 76830 | 84801 | 92515 | 94123  | 95387  | 90513 | 83936 | 85593 | 73763 | 62424 | 58688 |
| 15   | 52868 | 61647 | 70395 | 78658 | 80750  | 82740  | 83254 | 72209 | 72169 | 58536 | 48323 | 45185 |
| 16   | 32851 | 41258 | 51121 | 59948 | 61721  | 66347  | 63359 | 52871 | 53418 | 39136 | 29224 | 26890 |
| 17   | 11093 | 18678 | 27870 | 36777 | 39455  | 45644  | 41650 | 33952 | 29821 | 16403 | 8884  | 7142  |

Table 7. Average diffuse horizontal illuminance (lx)

| Hour | Jan   | Feb   | Mar   | Apr   | May   | Jun   | Jul   | Aug   | Sep   | Oct   | Nov   | Dec   |
|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 8    | 8257  | 11205 | 14001 | 17611 | 16751 | 17543 | 15628 | 12705 | 14779 | 6959  | 6781  | 5826  |
| 9    | 12903 | 15385 | 17355 | 19119 | 18570 | 20102 | 19178 | 13968 | 17523 | 10189 | 9312  | 8212  |
| 10   | 15459 | 17618 | 19234 | 20908 | 19912 | 20366 | 22100 | 20408 | 18974 | 16644 | 11265 | 8999  |
| 11   | 17075 | 18699 | 20265 | 22252 | 21027 | 20092 | 25620 | 22435 | 19854 | 18593 | 15399 | 11802 |
| 12   | 17594 | 19064 | 19983 | 22708 | 21724 | 20959 | 26986 | 23821 | 19771 | 19753 | 19483 | 19839 |
| 13   | 19055 | 19684 | 20140 | 23058 | 22230 | 23147 | 27318 | 25351 | 20866 | 20687 | 18918 | 19802 |
| 14   | 18293 | 19216 | 20341 | 23090 | 22606 | 23155 | 26203 | 25515 | 21893 | 19612 | 18670 | 17162 |
| 15   | 16354 | 17832 | 19123 | 22123 | 22148 | 23419 | 23986 | 23316 | 20908 | 17424 | 16827 | 15599 |
| 16   | 13773 | 15241 | 17064 | 20764 | 21597 | 20018 | 21035 | 18361 | 17968 | 13994 | 13423 | 12136 |
| 17   | 6528  | 9941  | 13133 | 17228 | 19528 | 17126 | 16422 | 14162 | 13970 | 9351  | 6759  | 5812  |

From Figure 6 it can be seen that above 90% of the time in a year there is availability of diffuse illuminance of 15,000 lx, which is significant because diffuse illuminance is glare free.

To accurately estimate daylight in the interiors it is required to estimate daylight availability outdoors at the four walls of a room. Therefore, slope exterior illuminance was estimated for the June average day and January average day for four orientations (N, E, S and W).

Figures 7 and 8 show the monthly average hourly global illuminance and diffuse illuminance, respectively, for June. It is observed from Figure 7 that due to higher solar altitude in June the horizontal surface receives much more global illuminance than vertical surfaces but the diffuse illuminance is about one and a half times of the vertical surfaces. Secondly due to low solar altitudes in the East and West walls the illuminance on East facing surface during morning and the west-facing surface during evening will be excessive which can create lot of glare. Both the global and diffuse illuminance at south wall is close to the illuminance in East wall during mornings and West wall during evenings as can be seen from Figures 7 and 8.

Similarly, monthly average hourly global illuminance and diffuse illuminance, respectively, for January were estimated and then plotted as shown in Figures 9 and 10. Due to lower inclination angles at the southern facade about 44° at noon the global illuminance at the Southern facade is higher than horizontal illuminance. So a southern facade can be benefited by the diffuse illuminance if an overhang cuts the beam component.

From Figures 9 and 10 the differences in illuminance level, which occur with orientation for both global and diffuse, can be seen. Although the North and South surfaces both peak at noon but global and diffuse illuminance for North surface is less than one fifth and one third of South plane, respectively. Although the illuminance on all the surfaces is higher in January than in June but the illuminance at lower solar altitudes is lower in January at the North plane.

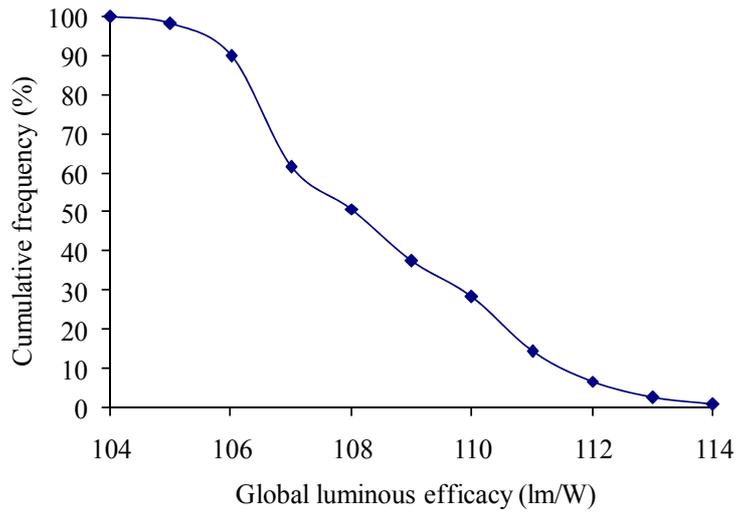


Figure 1. Cumulative frequency distribution for global luminous efficacy

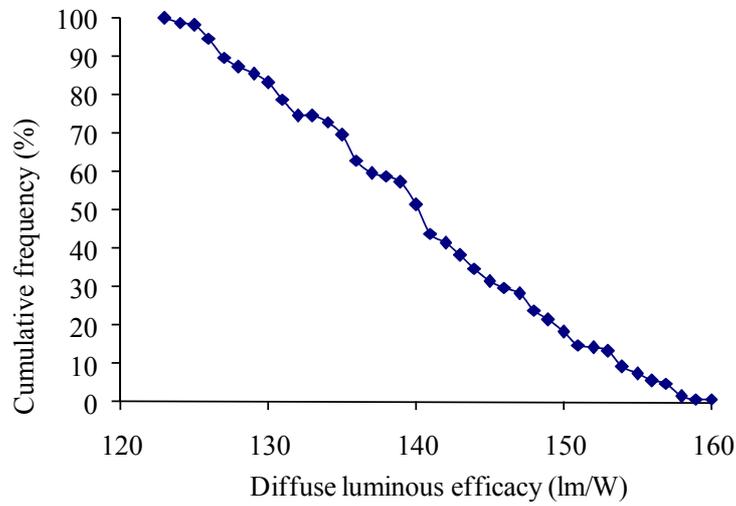


Figure 2. Cumulative frequency distribution for diffuse luminous efficacy

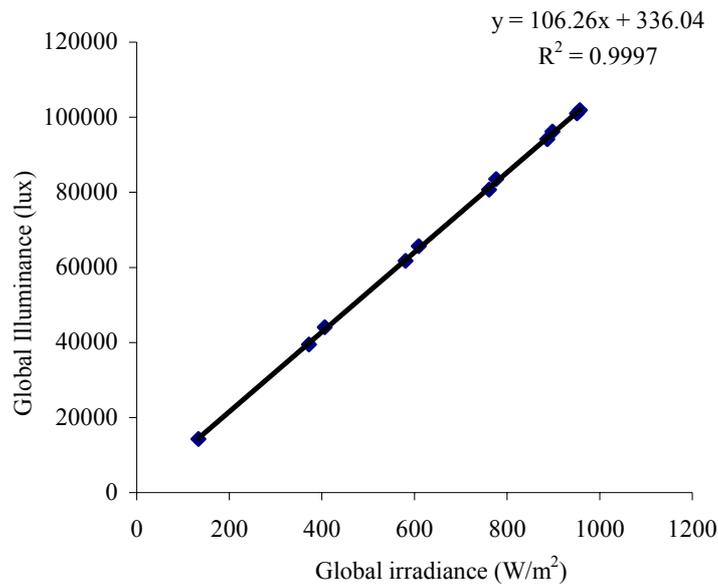


Figure 3. Graph of global illuminance against global irradiance for New Delhi, India

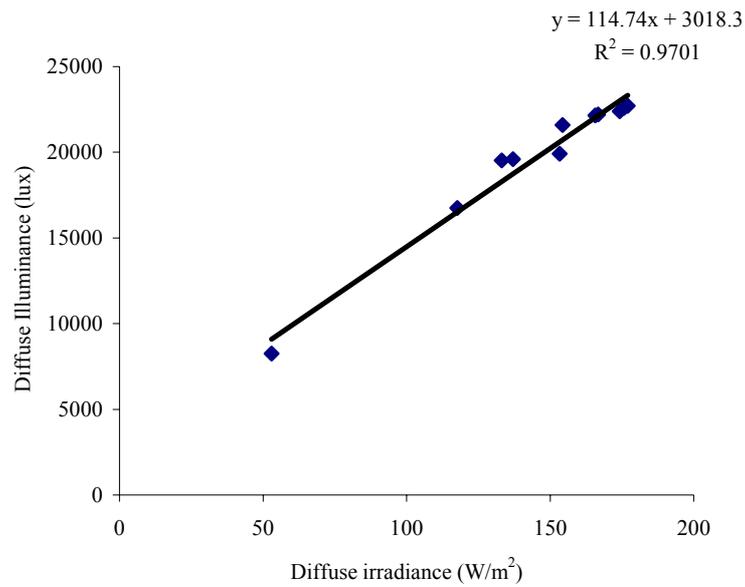


Figure 4. Graph of diffuse illuminance against diffuse irradiance for New Delhi, India

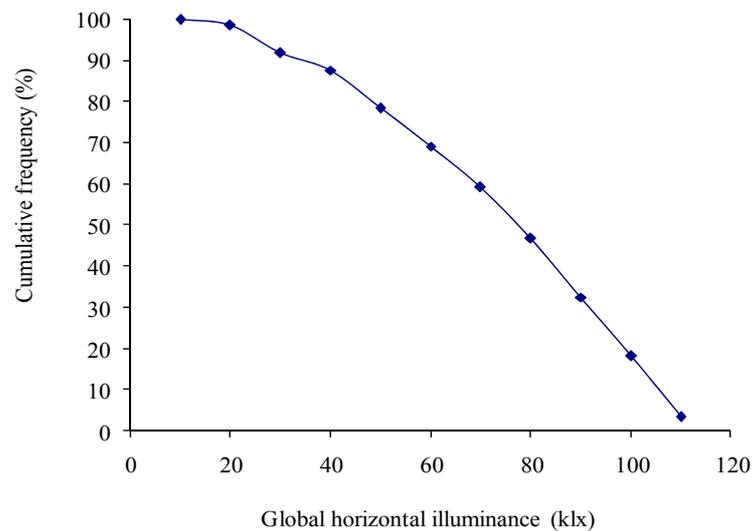


Figure 5. Cumulative frequency distribution for estimated outdoor global illuminance

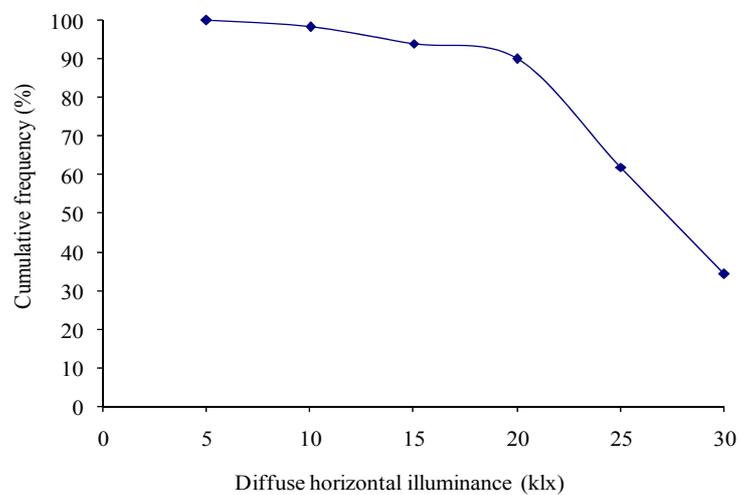


Figure 6. Cumulative frequency distribution for estimated outdoor diffuse illuminance

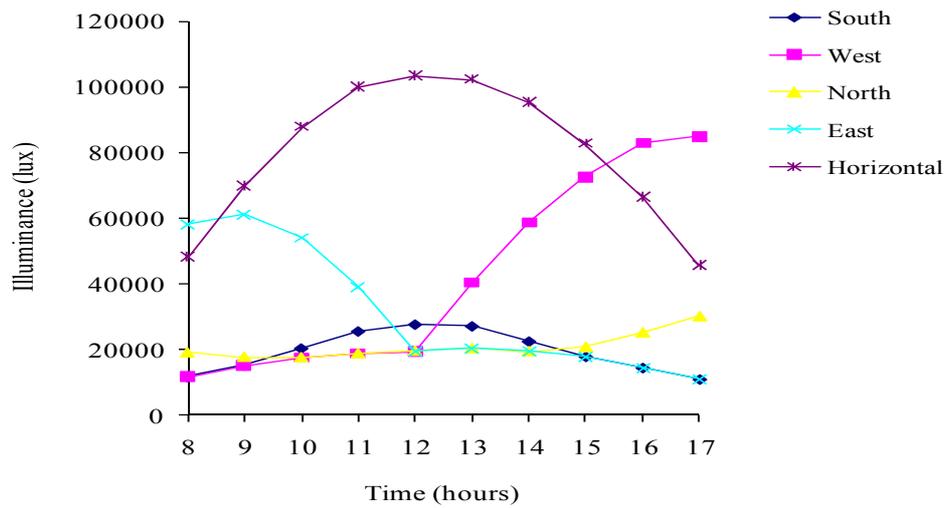


Figure 7. Average global illuminance for horizontal and four vertical surfaces in June

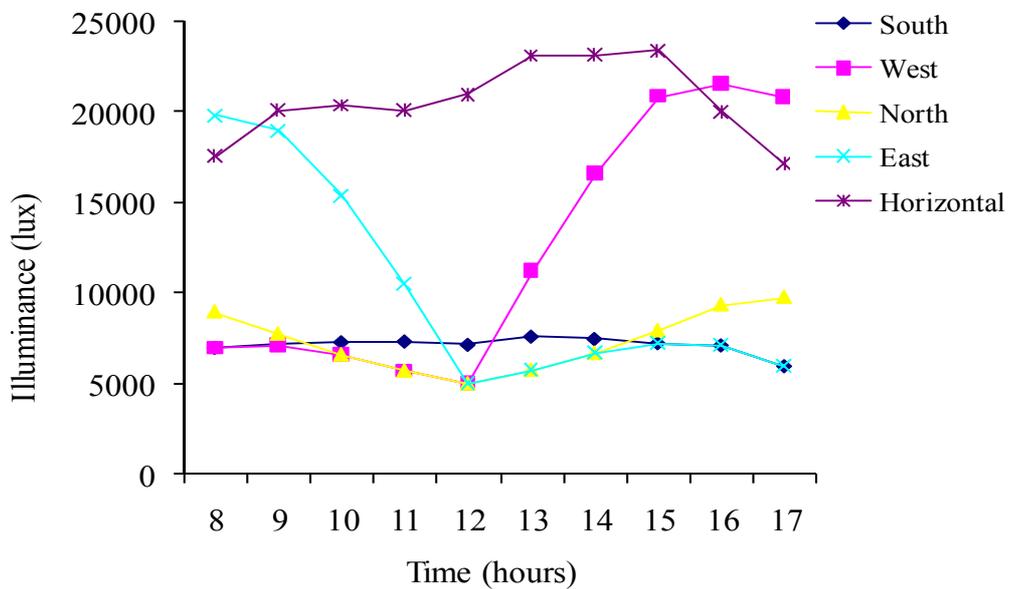


Figure 8. Average diffuse illuminance for horizontal and four vertical surfaces in June

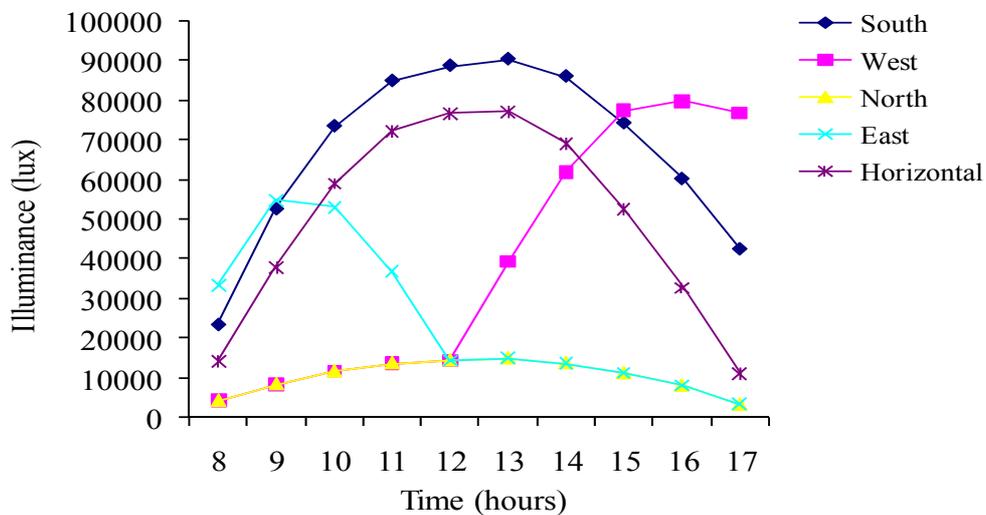


Figure 9. Average global illuminance for horizontal and four vertical surfaces in January

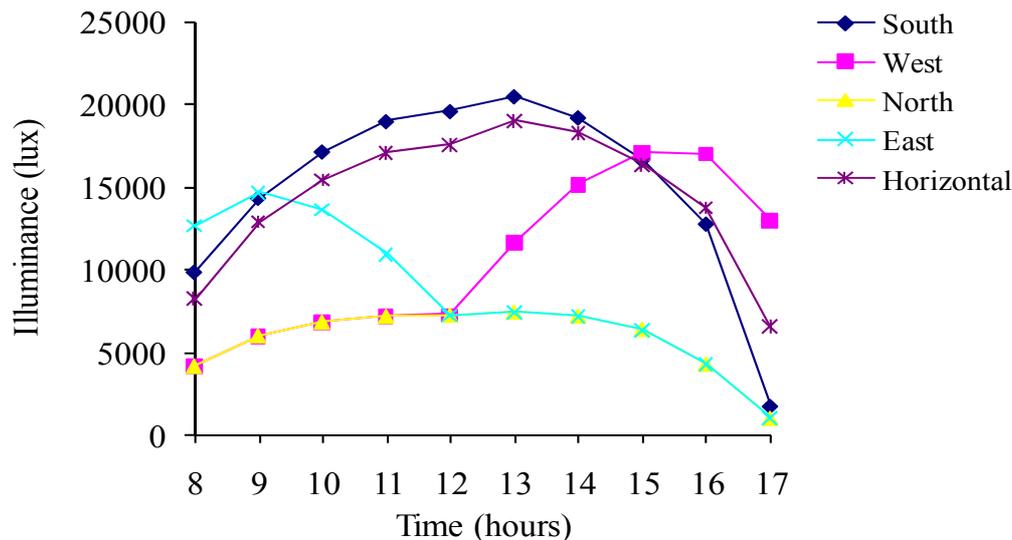


Figure10. Average diffuse illuminance for horizontal and four vertical surfaces in January

## 6. Average global and diffuse illuminance

For determination of maximum illuminance level the hourly illuminance data for the horizontal surface and the four vertical surfaces were used. Tables 8 and 9 present the average illuminance on horizontal and four vertical surfaces. For the months of November, December, January and February the peak average illuminance occurs on the Southern facade because of low solar inclination on the South facade during these months and for the other months the peak occurs in the horizontal plane. Because of maximum solar altitude in June, the maximum horizontal illuminance occurs in June. The illuminance on East and west planes is like sinusoidal. For vertical surfaces the highest global illuminance occurs in January for a south-facing surface and the lowest occurs for the North-facing surface in December. The maximum diffuse illuminance occurs in January for a South-facing surface, which is because of composite weather conditions in the region while the minimum occurs for the North facing surfaces during winters since the sun moves to southward direction during this period.

Figure 11 presents the cumulative frequency distributions for the hourly global illuminances for the horizontal and four vertical places based on normal office hour of 08.0–17.0. The effects of inclination can be observed. The horizontal illuminance is around one and a half times of the vertical illuminance. It can be seen that the horizontal surface receives the largest amount of illuminance with a peak value of 103,353 lx in June. The north-facing surface has the lowest illuminance among all the vertical surfaces with the peak value being around 30 klx. The East and West facing surfaces touch their peaks at around 61 klx and 84 klx respectively while the South-facing surface has its peak at 90 klx which is three times than that of North facing surface. It can be pointed out that the North-facing surface receives mainly diffuse component of the total illuminance so no shading device is required to exclude the direct component. It can also be noted that at low illuminance levels of around 15 klx and less, the North and East-facing surfaces show similar trends in illumination. Results obtained are in good agreement with results obtained by other similar study [17].

## 7. Validation of interior illuminance model using experimental performance of skylight

Figure 12 shows the different types of skylight for daylighting of building as reported by Laouadi and Atif [18]. The existing mud-house has vault (or dome shape) roof structure as shown by the pictorial view of skylight dome in Figure 13 shows the schematic diagram of dome shape skylight rooms. There are three numbers of dome shape roof structure rooms out of which two rooms have identical small dome shape rooms with skylight at central height of about 3 m while the large dome shape room has skylight at central height about 7 m. The wall of the dome shape rooms forms regular octagonal base for the dome roof structure. The eight rectangular walls of the big dome shape room have width 2.32 m and height 2.32 m. The dome was constructed over these eight walls.

The experimental measurements were carried out on hourly basis at working levels (75 cm above ground) inside the room. The skylight building is used as conference room which also provides the computer simulation laboratory for the solar energy scientists.

The illuminance level inside the dome shaped room with skylight was practically found suitable for reading and writing from 7 am to 5 pm (daytime). The illuminance level inside the big dome on typical clear days in months of March and April are shown in Figure 14. The value of predicted interior illuminance was determined using following Equation.

$$A_g \times I_g \times \tau \times \rho \times 100 = L_i \times A_f \quad (27)$$

where  $A_g$  is total area of glazing,  $\tau$  is transmittance of glazing,  $\rho$  is average reflectance of all room-surfaces,  $L_i$  is illuminance level inside the room on horizontal working surface (Lux or  $\text{lm/m}^2$ ), and  $A_f$  is floor area.

Parametric values considered for evaluation of interior illuminance are given in Table 10. Figure 14 shows the experimental validation of interior illuminance model which was used to determine hourly illuminance value inside the big and small rooms. The validation results show that root mean square percentage error varies in the range of 4.5 – 9.66% while the correlation coefficient varies in the range of 0.9 -0.99. The statistical error represented in Figure 14 are within the acceptable limits and hence the proposed model estimation of interior illuminance can be used for estimation of interior illuminance based on the experimental results conducted in the existing building in New Delhi (India). Figure 15 shows the hourly variation of predicted interior illuminance based on Eq (27).

Table 8. Average global illuminance for New Delhi (lux)

| Period | South | West  | North | East  | Horizontal |
|--------|-------|-------|-------|-------|------------|
| Jan    | 67822 | 38850 | 10361 | 24387 | 50468      |
| Feb    | 57686 | 43605 | 11798 | 25244 | 56782      |
| Mar    | 45614 | 43919 | 13514 | 27940 | 65607      |
| Apr    | 32569 | 43756 | 15895 | 30955 | 74548      |
| May    | 22369 | 40676 | 17879 | 30707 | 76836      |
| Jun    | 19294 | 42159 | 20717 | 31426 | 80166      |
| Jul    | 20665 | 41367 | 19806 | 30462 | 75458      |
| Aug    | 25817 | 38412 | 15833 | 29551 | 69205      |
| Sep    | 39884 | 42399 | 14337 | 28778 | 68283      |
| Oct    | 48940 | 37405 | 11366 | 24637 | 54725      |
| Nov    | 56404 | 34217 | 9618  | 22374 | 45550      |
| Dec    | 64042 | 40737 | 8740  | 20928 | 41837      |

Table 9. Average diffuse illuminance for New Delhi (lux)

| Period | South | West  | North | East  | Horizontal |
|--------|-------|-------|-------|-------|------------|
| Jan    | 15031 | 10526 | 5760  | 8555  | 14529      |
| Feb    | 15017 | 11380 | 6229  | 9520  | 16388      |
| Mar    | 13391 | 12174 | 6593  | 10304 | 18064      |
| Apr    | 10806 | 12926 | 6662  | 10744 | 20886      |
| May    | 8007  | 12585 | 6899  | 10195 | 20609      |
| Jun    | 7084  | 12226 | 7311  | 10208 | 20593      |
| Jul    | 7567  | 12505 | 6952  | 10204 | 22448      |
| Aug    | 9476  | 12401 | 6507  | 9768  | 20004      |
| Sep    | 12324 | 12427 | 6598  | 10336 | 18651      |
| Oct    | 13679 | 11108 | 6084  | 8640  | 15321      |
| Nov    | 14149 | 9898  | 5510  | 7726  | 13684      |
| Dec    | 15005 | 9407  | 5653  | 7775  | 12519      |

Table 10. Parametric values considered for evaluation of interior illuminance

| No. | Parameter   | Value |
|-----|---|-------|
| 1   | Floor area of room under big dome ( $A_f$ , m <sup>2</sup> )    | 26    |
| 2   | Floor area of room under small dome ( $A_f$ , m <sup>2</sup> )  | 5     |
| 3   | Total area of glazing ( $A_g$ , m <sup>2</sup> ) for big dome   | 2.6   |
| 4   | Total area of glazing ( $A_g$ , m <sup>2</sup> ) for small dome | 1.5   |
| 5   | Transmittance of glazing ( $\tau$ )                             | 0.5   |
| 6   | Average reflectance ( $\rho$ ) of all room surfaces             | 0.4   |

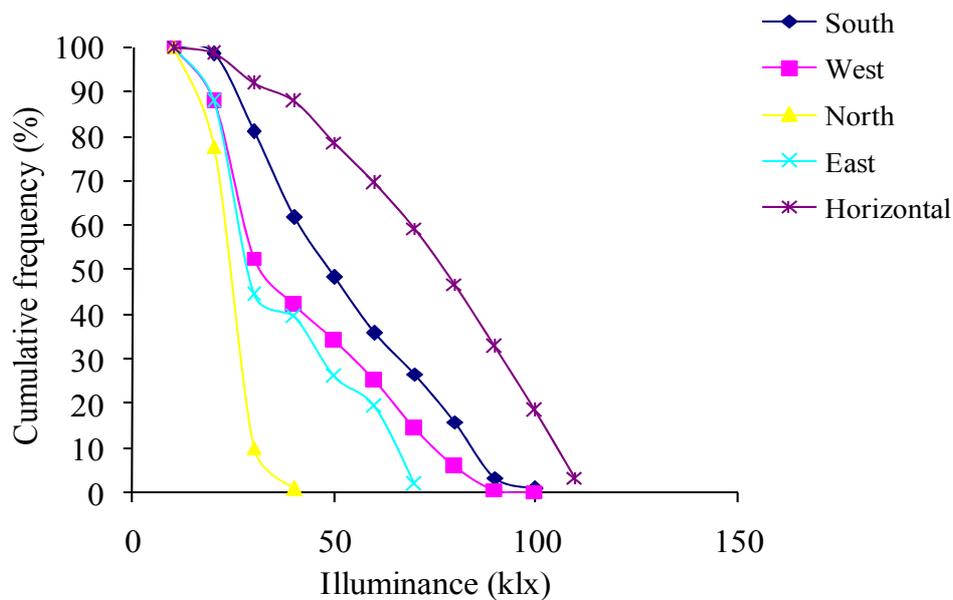


Figure 11. Cumulative frequency distribution for the hourly global illuminances for the horizontal and four vertical places

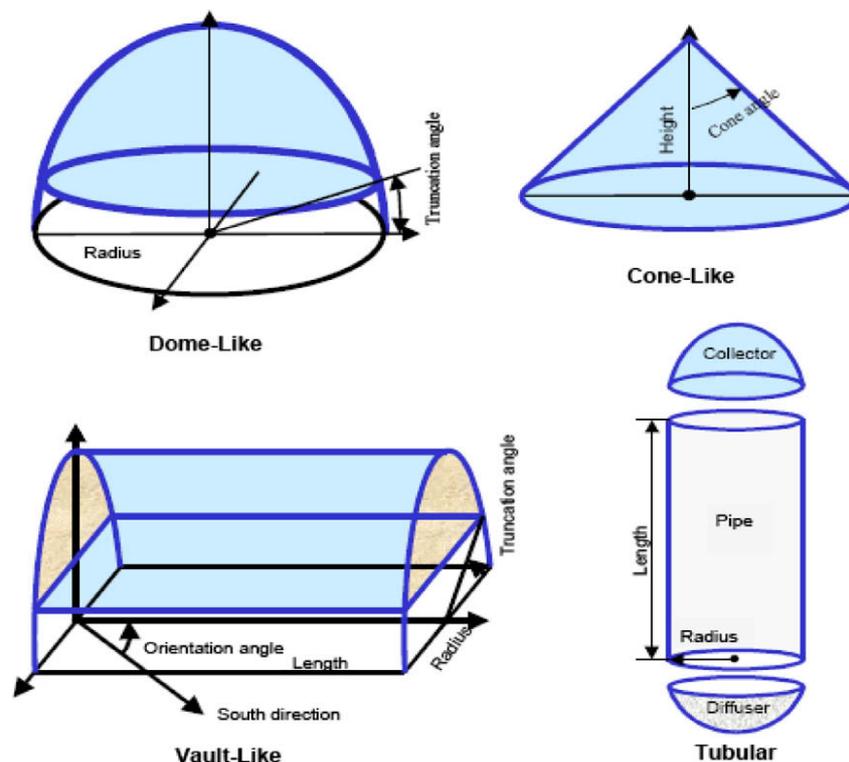


Figure 12. Types of skylight for daylighting in buildings (Laouadi and Atif [18])

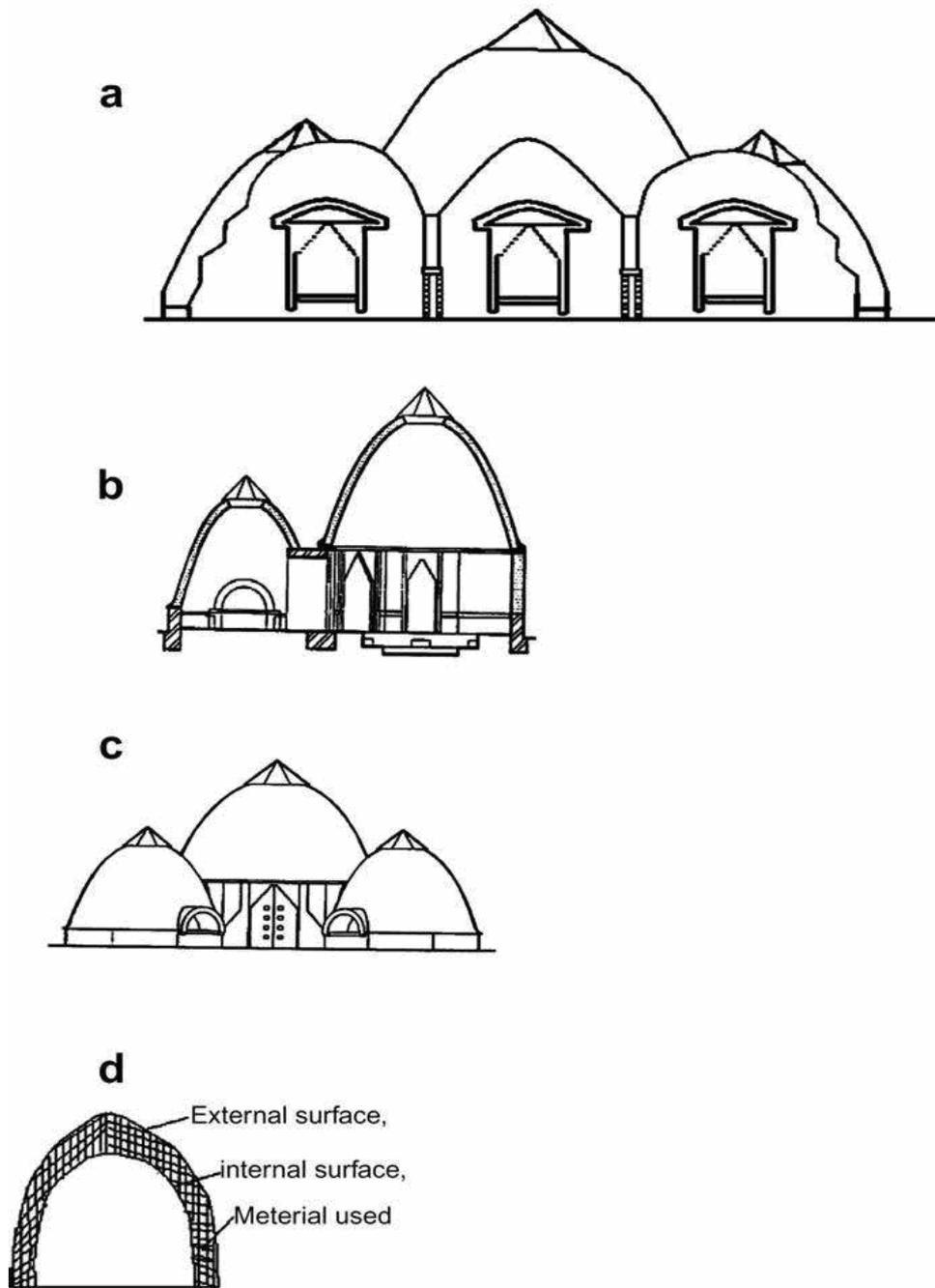


Figure 13. Adobe house (a) front view (b) side view (c) rear view (d) schematic diagram for material calculation

### 8. Mitigation of CO<sub>2</sub> emission

The mitigation of CO<sub>2</sub> emission from the energy saving potential and corresponding amount of carbon credit potential of the skylight for big and small dome room was estimated to promote daylighting issue in buildings. The CO<sub>2</sub> emission intensity at coal thermal power plant in India was estimated as 1.568 kg/kW h of electrical energy generated as reported by Watt et al [19]. The mitigation of CO<sub>2</sub> emission from the actual amount of lighting energy saving potential due to skylight can be determined using the relation reported by Watt et al [19] as follows:

$$\text{Mitigation of CO}_2 \text{ emissions} = \text{Energy saving (kWh/year)} \times 1.568 \text{ (kg of CO}_2 \text{/kWh)} \quad (28)$$

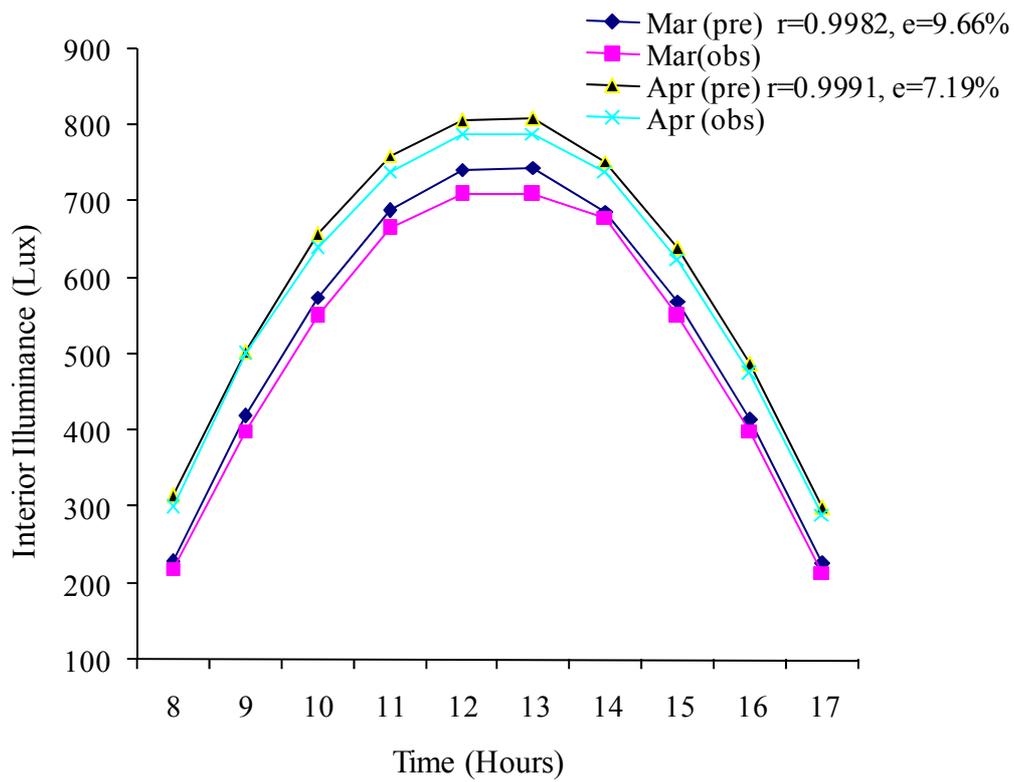


Figure 14. Hourly variation of predicted and observed interior illuminance

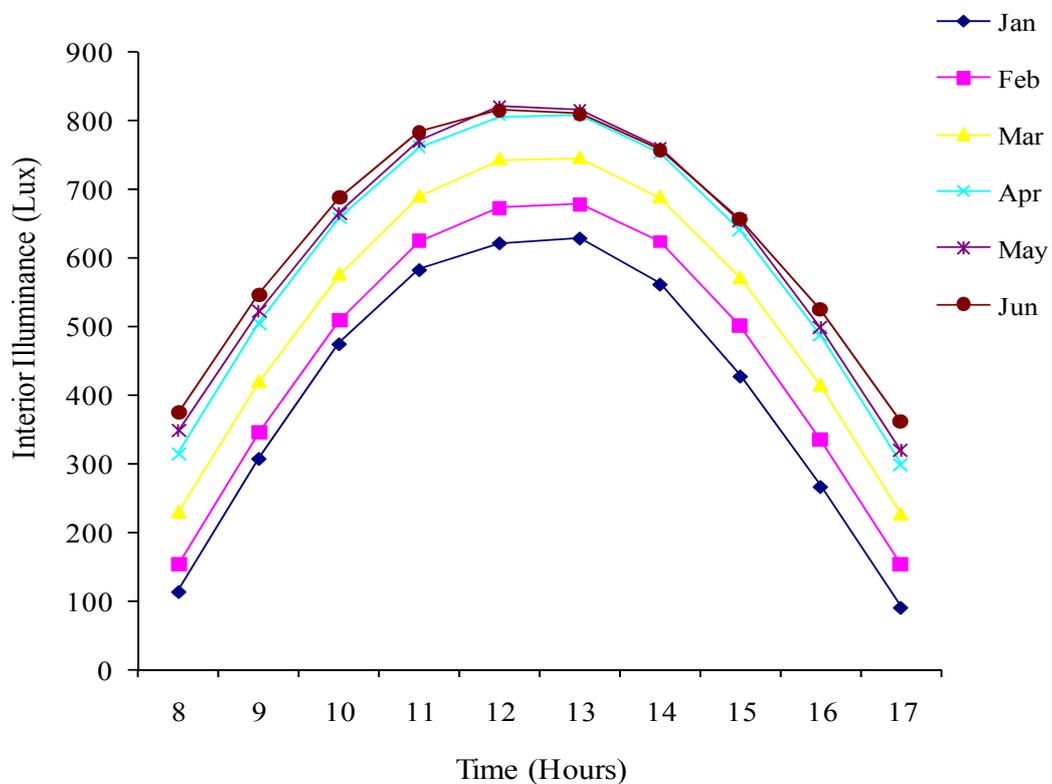


Figure 15. (a) Hourly variation of interior illuminance from January to June months

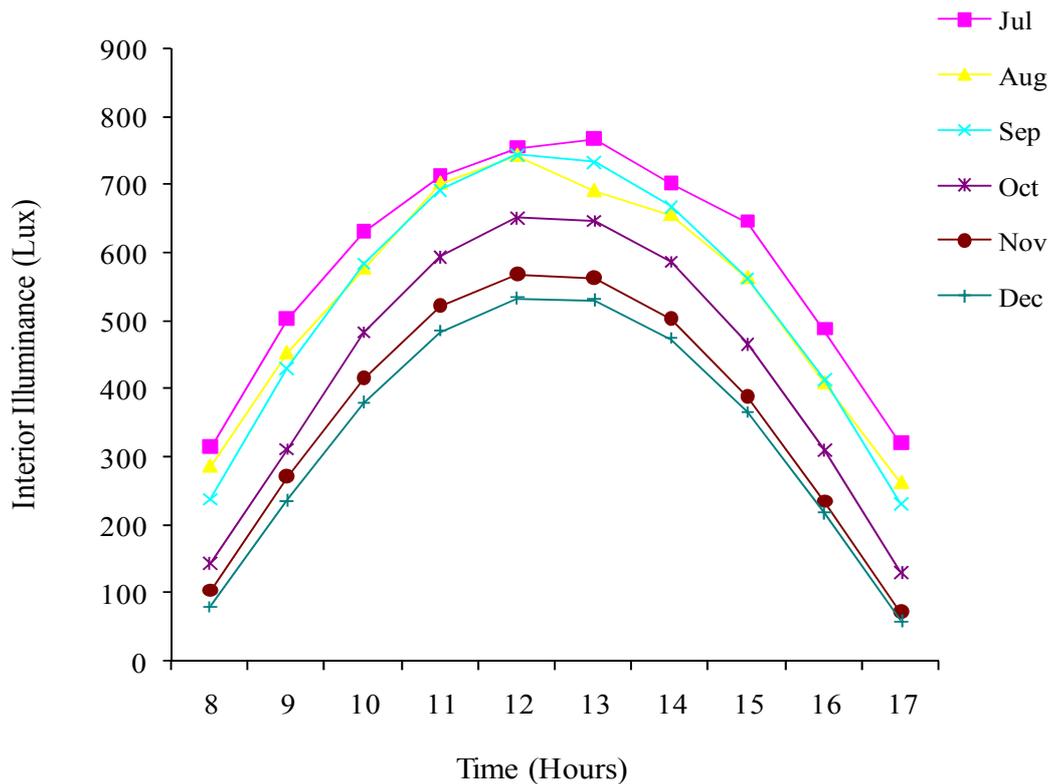


Figure 15. (b) Hourly variation of interior illuminance from July to December months

### 9. Carbon credit earned from mitigation of CO<sub>2</sub> emission

The carbon credit earned from the mitigation of CO<sub>2</sub> emissions (in tons/year) can be determined using the relation as follows [19, 20]:

$$\text{Carbon credit earned} = \text{Mitigation of CO}_2 \text{ emissions (tons/year)} \times 21 \text{ (Euro/ton of CO}_2\text{)} \quad (29)$$

The factor considered in Eq. (29) is 21 Euro (€)/metric tons of CO<sub>2</sub> mitigation in Asia (especially in India) [19] represents the monetary value of one carbon credit earned due to mitigation of 1 metric ton of CO<sub>2</sub> emissions due to skylight for natural daylighting inside the room.

### 10. Conclusion

This study was a step towards predicting the illuminance in buildings in India. It is evident that the South wall has the highest daylight availability during winter, which is desirable from it during these months. So buildings oriented South can not only be benefited by daylight but also by warmth during this period in the area. It is also evident that the global luminous efficacy can lie at 108.0 lm/W in the area and the diffuse luminous efficacy can lie between 136.5 lm/W, which is close to established values. The maximum horizontal illuminance of 70,000 lx is exceeded in the area for most of the months touching the maximum of 103,353 lx in June. This approach is particularly useful for estimating the illuminance of different daylighting schemes during the conceptual design stage. The north-facing wall mainly receives the diffuse component of illuminance values while the horizontal and other vertical surfaces receive certain amount of direct component. The information of percentage of working period in which a given illuminance is exceeded is valuable in designing the building for specific interior illumination.

The interior illuminance model to determine inside illuminance of the skylight building was found in good agreement with experimental results of skylight building at working level of interest (75 cm above floor level) for both small and big dome rooms. Also, the methodology to calculate energy saving potential of daylighting showed that tremendous amount of energy can be conserved from skylight integrated buildings if adopted in both rural and urban areas of India. The skylights were found to provide diffuse light and not the direct light based on the experimental observations. The direct light provides undesirable glare and heating effect inside the room. Hence, daylight are often termed as cool light to provide illumination for the given task of human being such as reading, writing, drawing, etc.

The emission reduction and carbon credit potential were discussed to signify daylighting as one of the environment friendly sustainable approach for buildings. The Indian government had planned to adopt green rating for integrated habitat assessment (GRIHA) for all new buildings. This will be made mandatory for the commercial buildings which consume 100 kW of power or more in 1 h [21]. The daylighting is one of the important building codes defined by GRIHA for building rating system in India. With the advent of this rating system, day-lighting in buildings will be made mandatory for commercial complexes to reduce lighting-energy-consumption of buildings. The integration of artificial lights with natural light is desirable for effective utilization of daylighting in buildings.

## Appendix

Horizontal irradiance for New Delhi, W/m<sup>2</sup>

| Solar Radiation | Month   | January | February | March  | April  | May    | June   | July   | August | September | October | November | December |        |
|-----------------|---------|---------|----------|--------|--------|--------|--------|--------|--------|-----------|---------|----------|----------|--------|
| Global          | 8am     | 132.99  | 180.29   | 266.77 | 368.14 | 406.31 | 436.67 | 367.36 | 333.59 | 277.96    | 168.75  | 121.46   | 93.12    |        |
|                 | 9am     | 355.56  | 403.58   | 488.94 | 588.48 | 608.84 | 637.22 | 587.04 | 528.54 | 501.3     | 364.58  | 316.04   | 275.27   |        |
|                 | 10am    | 554.69  | 594.44   | 671.21 | 767.81 | 776.26 | 802.22 | 737.27 | 674.49 | 682.04    | 565.28  | 485.35   | 443.25   |        |
|                 | 11am    | 680.73  | 729.39   | 804.33 | 888.32 | 897.98 | 915    | 831.71 | 820.2  | 809.07    | 694.45  | 609.97   | 565.87   |        |
|                 | 12pm    | 726.74  | 786.02   | 866.93 | 941.01 | 956.82 | 951.67 | 881.48 | 868.18 | 869.07    | 761.8   | 664.01   | 621.83   |        |
|                 | 1pm     | 733.85  | 792.03   | 869.28 | 944.12 | 950.51 | 946.11 | 896.53 | 807.83 | 855.19    | 756.25  | 657.45   | 618.39   |        |
|                 | 2pm     | 656.08  | 728.58   | 803.15 | 878.68 | 886.62 | 882.78 | 820.6  | 766.67 | 779.81    | 686.11  | 587.37   | 553.31   |        |
|                 | 3pm     | 500     | 584.23   | 665.33 | 746.9  | 761.37 | 765.56 | 753.24 | 658.08 | 656.48    | 543.75  | 454.17   | 426.19   |        |
|                 | 4pm     | 311.46  | 391.22   | 483.01 | 568.3  | 580.81 | 611.67 | 569.68 | 477.78 | 483.89    | 362.5   | 274.62   | 253.97   |        |
|                 | 5pm     | 106.42  | 178.23   | 264.1  | 348.61 | 372.48 | 420    | 373.15 | 305.81 | 270.19    | 152.08  | 84.09    | 68.78    |        |
|                 | Diffuse | 8am     | 52.6     | 73.3   | 94.23  | 122.47 | 117.68 | 123.89 | 109.03 | 86.62     | 100     | 44.44    | 42.8     | 36.37  |
|                 |         | 9am     | 86.28    | 105.82 | 123.02 | 139.54 | 137.12 | 149.44 | 141.44 | 100       | 124.81  | 68.75    | 61.36    | 53.31  |
|                 |         | 10am    | 107.29   | 126.08 | 142.2  | 159.4  | 153.28 | 157.22 | 171.07 | 155.3     | 140.93  | 119.45   | 77.15    | 60.19  |
|                 |         | 11am    | 121.53   | 137.36 | 154.11 | 174.84 | 166.67 | 158.89 | 205.09 | 176.26    | 151.67  | 137.5    | 109.6    | 81.61  |
|                 |         | 12pm    | 126.39   | 141.31 | 153.21 | 180.39 | 174.24 | 167.78 | 218.75 | 189.65    | 152.41  | 147.92   | 141.67   | 142.46 |
| 1pm             |         | 136.63  | 145.07   | 153.21 | 181.78 | 177.02 | 185    | 219.68 | 201.26 | 160       | 154.17  | 136.36   | 141.27   |        |
| 2pm             |         | 128.3   | 138.35   | 151.12 | 177.45 | 175.76 | 180.56 | 204.86 | 197.48 | 164.26    | 142.36  | 131.82   | 119.18   |        |
| 3pm             |         | 110.94  | 123.84   | 136.54 | 163.24 | 165.66 | 176.11 | 179.63 | 172.72 | 150.74    | 121.53  | 114.77   | 105.03   |        |
| 4pm             |         | 90.28   | 101.52   | 116.35 | 146.08 | 154.29 | 142.78 | 149.54 | 128.28 | 123.15    | 93.06   | 88.01    | 78.84    |        |
| 5pm             |         | 41.84   | 63.98    | 85.74  | 115.36 | 133.08 | 116.11 | 110.42 | 93.69  | 91.3      | 59.72   | 43.05    | 37.43    |        |

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